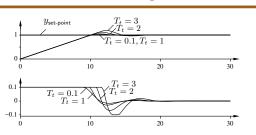


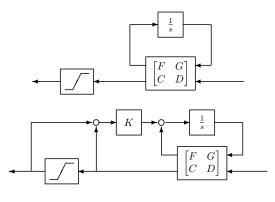
Choice of Tracking Time T_t



With very small T_t (large gain $1/T_t$), spurious errors can saturate the output, which leads to accidental reset of the integrator. Too large T_t gives too slow reaction (little effect).

The tracking time T_t is the design parameter of the anti-windup. Common choices: $T_t = T_i$ or $T_t = \sqrt{T_i T_d}$.

State-space controller without and with anti-windup:



Antiwindup – General State-Space Controller

Mimic the observer-based controller:

$$\dot{x}_c = Fx_c + Gy + K \underbrace{(u - Cx_c - Dy)}_{=0}$$

$$= (F - KC)x_c + (G - KD)y + Ku$$

$$= F_0x_c + G_0y + Ku$$

Design so that ${\cal F}_0={\cal F}-KC$ has desired stable eigenvalues Then use controller

$$\begin{aligned} \dot{x}_c &= F_0 x_c + G_0 y + K u \\ u &= \text{sat} \left(C x_c + D y \right) \end{aligned}$$

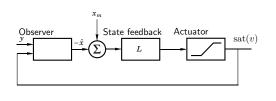
Saturation

Optimal control theory (later)

Multi-loop Anti-windup (Cascaded systems):

Difficult problem, several suggested solutions Turn off integrator in outer loop when inner loop saturates

State feedback with Observer



$$\hat{x} = A\hat{x} + B\operatorname{sat}(v) + K(y - C\hat{x})$$
$$v = L(x_m - \hat{x})$$

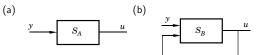
 \hat{x} is estimate of process state, x_m desired (model) state. Need model of saturation if $\mathrm{sat}(v)$ is not measurable

Antiwindup – General State-Space Controller

State-space controller:

$$\begin{aligned} \dot{x}_c(t) &= F x_c(t) + G y(t) \\ u(t) &= C x_c(t) + D y(t) \end{aligned}$$

Windup possible if F is unstable and u saturates.



Idea:

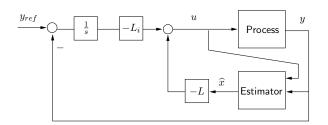
Rewrite representation of control law from (a) to (b) such that:

(a) and (b) have same input-output relation

(b) behaves better when feedback loop is broken, if ${\cal S}_{\cal B}$ stable

5 Minute Exercise

How would you do antiwindup for the following state-feedback controller with observer and integral action ?



Friction

Present almost everywhere

- Often bad
 - Friction in valves and mechanical constructions
 - Sometimes good
 - Friction in brakesSometimes too small
 - Earthquakes

Problems

- How to model friction
- ▶ How to compensate for friction

