Deep RL with Q-Functions

CS 285: Deep Reinforcement Learning, Decision Making, and Control Sergey Levine

Class Notes

- 1. Homework 2 is due next Monday
- 2. Project proposal due 9/25, that's today!
 - Remember to upload to **both** Gradescope and CMT (see Piazza post)

Today's Lecture

- 1. How we can make Q-learning work with deep networks
- 2. A generalized view of Q-learning algorithms
- 3. Tricks for improving Q-learning in practice
- 4. Continuous Q-learning methods
- Goals:
 - Understand how to implement Q-learning so that it can be used with complex function approximators
 - Understand how to extend Q-learning to continuous actions

Recap: Q-learning

full fitted Q-iteration algorithm:

1. collect dataset $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy 2. set $\mathbf{y}_i \leftarrow r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'_i} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)$ 3. set $\phi \leftarrow \arg \min_{\phi} \frac{1}{2} \sum_i \|Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - \mathbf{y}_i\|^2$

online Q iteration algorithm:



What's wrong?

online Q iteration algorithm:

1. take some action
$$\mathbf{a}_i$$
 and observe $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$
2. $\mathbf{y}_i = r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)$
3. $\phi \leftarrow \phi - \alpha \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - \mathbf{y}_i)$
isn't this just gradient descent? that converges, right?

Q-learning is *not* gradient descent!

$$\phi \leftarrow \phi - \alpha \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - \mathbf{r}(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)])$$

no gradient through target value

Correlated samples in online Q-learning

online Q iteration algorithm:

1. take some action a_i and observe (s_i, a_i, s'_i, r_i) - target value
 2. φ ← φ − α dQ_φ/dφ (s_i, a_i) (Q_φ(s_i, a_i) − [r(s_i, a_i) + γ max_{a'} Q_φ(s'_i, a'_i)])



asynchronous parallel Q-learning

- sequential states are strongly correlated

- target value is always changing

synchronized parallel Q-learning





Another solution: replay buffers

online Q iteration algorithm:

1. take some action \mathbf{a}_i and observe $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$ 2. $\phi \leftarrow \phi - \alpha \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)])$

full fitted Q-iteration algorithm:

1. collect dataset $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy $K \times 2. \text{ set } \mathbf{y}_i \leftarrow r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'_i} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)$ $3. \text{ set } \phi \leftarrow \arg \min_{\phi} \frac{1}{2} \sum_i \|Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - \mathbf{y}_i\|^2$ any policy will work! (with broad support) just load data from a buffer here still use one gradient step



special case with K = 1, and one gradient step

Another solution: replay buffers

Q-learning with a replay buffer:

+ samples are no longer correlated

1. sample a batch $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$ from \mathcal{B} 2. $\phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)])$

+ multiple samples in the batch (low-variance gradient)

but where does the data come from?

need to periodically feed the replay buffer...



Putting it together

full Q-learning with replay buffer:

1. collect dataset $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add it to \mathcal{B}

 $K \times \begin{cases} 2. \text{ sample a batch } (\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i) \text{ from } \mathcal{B} \\ 3. \phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi} (\mathbf{s}_i, \mathbf{a}_i) (Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)]) \end{cases}$

K = 1 is common, though larger K more efficient



What's wrong?

online Q iteration algorithm:

1. take some action
$$\mathbf{a}_i$$
 and observe $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$
2. $\mathbf{y}_i = r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)$
3. $\phi \leftarrow \phi - \alpha \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - \mathbf{y}_i)$
use replay buffer

Q-learning is *not* gradient descent!

$$\phi \leftarrow \phi - \alpha \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_{i}, \mathbf{a}_{i})(Q_{\phi}(\mathbf{s}_{i}, \mathbf{a}_{i}) - \mathbf{r}(\mathbf{s}_{i}, \mathbf{a}_{i}) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_{i}, \mathbf{a}'_{i})])$$
This is still a problem!

Q-Learning and Regression

full Q-learning with replay buffer:

1. collect dataset $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add it to \mathcal{B}

 $K \times \begin{cases} 2. \text{ sample a batch } (\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i) \text{ from } \mathcal{B} \\ 3. \phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi} (\mathbf{s}_i, \mathbf{a}_i) (Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)]) \end{cases}$

one gradient step, moving target

full fitted Q-iteration algorithm:

1. collect dataset
$$\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$$
 using some policy
2. set $\mathbf{y}_i \leftarrow r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'_i} Q_{\phi}(\mathbf{s}'_i, \mathbf{a}'_i)$
3. set $\phi \leftarrow \arg \min_{\phi} \frac{1}{2} \sum_i ||Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - \mathbf{y}_i||^2$

perfectly well-defined, stable regression

Q-Learning with target networks

Q-learning with replay buffer and target network:

→ 1. save target network parameters:
$$\phi' \leftarrow \phi$$

▶ 2. collect dataset $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add it to \mathcal{B}

$$\times$$
 \rightarrow 3. sample a batch $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$ from \mathcal{B}

4.
$$\phi \leftarrow \phi - \alpha \sum_{i} \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_{i}, \mathbf{a}_{i})(Q_{\phi}(\mathbf{s}_{i}, \mathbf{a}_{i}) - [r(\mathbf{s}_{i}, \mathbf{a}_{i}) + \gamma \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}'_{i}, \mathbf{a}'_{i})]$$

targets don't change in inner loop!

"Classic" deep Q-learning algorithm (DQN)

Q-learning with replay buffer and target network:

1. save target network parameters:
$$\phi' \leftarrow \phi$$

2. collect dataset $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add it to \mathcal{B}
 $N \times \mathbf{s}$
3. sample a batch $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)$ from \mathcal{B}
4. $\phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}'_i, \mathbf{a}'_i)])$

"classic" deep Q-learning algorithm:

You'll implement this in HW3!

Alternative target network

"classic" deep Q-learning algorithm:



Feels weirdly uneven, can we always have the same lag?

Popular alternative (similar to Polyak averaging):

5. update $\phi': \phi' \leftarrow \tau \phi' + (1 - \tau)\phi$ $\tau = 0.999$ works well

Fitted Q-iteration and Q-learning

Q-learning with replay buffer and target network:

1. save target network parameters: $\phi' \leftarrow \phi$

DQN: N = 1, K = 1

2. collect M datapoints $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add them to \mathcal{B} $N \times \mathbf{A} \times \mathbf{A}$ $K \times \mathbf{A}$ $4. \phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_i, \mathbf{a}_i)(Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}'_i, \mathbf{a}'_i)])$

Fitted Q-learning (written similarly as above):

→ 1. collect *M* datapoints $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add them to \mathcal{B}

▶ 2. save target network parameters:
$$\phi' \leftarrow \phi$$

$$N \times K \times 3. \text{ sample a batch } (\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i) \text{ from } \mathcal{B}$$

$$4. \phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi} (\mathbf{s}_i, \mathbf{a}_i) (Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}'_i, \mathbf{a}'_i)])$$
just SGD

A more general view

Q-learning with replay buffer and target network:

1. save target network parameters: $\phi' \leftarrow \phi$

2. collect *M* datapoints $\{(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i)\}$ using some policy, add them to \mathcal{B}

 $N \times \mathbf{K} \times 3. \text{ sample a batch } (\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}'_i, r_i) \text{ from } \mathcal{B}$ $4. \phi \leftarrow \phi - \alpha \sum_i \frac{dQ_{\phi}}{d\phi} (\mathbf{s}_i, \mathbf{a}_i) (Q_{\phi}(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}'_i, \mathbf{a}'_i)])$



A more general view



- Online Q-learning (last lecture): evict immediately, process 1, process 2, and process 3 all run at the same speed
- DQN: process 1 and process 3 run at the same speed, process 2 is slow
- Fitted Q-iteration: process 3 in the inner loop of process 2, which is in the inner loop of process 1

Break

Are the Q-values accurate?



As predicted Q increases, so does the return



Are the Q-values accurate?



Overestimation in Q-learning

target value $y_j = r_j + \gamma \max_{\mathbf{a}'_j} Q_{\phi'}(\mathbf{s}'_j, \mathbf{a}'_j)$ this last term is the problem

imagine we have two random variables: X_1 and X_2

 $E[\max(X_1, X_2)] \ge \max(E[X_1], E[X_2])$

 $Q_{\phi'}(\mathbf{s}', \mathbf{a}')$ is not perfect – it looks "noisy"

hence $\max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}', \mathbf{a}')$ overestimates the next value!

note that $\max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}', \mathbf{a}') = Q_{\phi'}(\mathbf{s}', \arg \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}', \mathbf{a}'))$

value *also* comes from $Q_{\phi'}$ action selected according to $Q_{\phi'}$

Double Q-learning

 $E[\max(X_1, X_2)] \ge \max(E[X_1], E[X_2])$

note that $\max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}', \mathbf{a}') = Q_{\phi'}(\mathbf{s}', \arg \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}', \mathbf{a}'))$ value also comes from $Q_{\phi'}$ action selected according to $Q_{\phi'}$ if the noise in these is decorrelated, the problem goes away!

idea: don't use the same network to choose the action and evaluate value!

"double" Q-learning: use two networks:

$$Q_{\phi_A}(\mathbf{s}, \mathbf{a}) \leftarrow r + \gamma Q_{\phi_B}(\mathbf{s}', \arg\max_{\mathbf{a}'} Q_{\phi_A}(\mathbf{s}', \mathbf{a}'))$$
$$Q_{\phi_B}(\mathbf{s}, \mathbf{a}) \leftarrow r + \gamma Q_{\phi_A}(\mathbf{s}', \arg\max_{\mathbf{a}'} Q_{\phi_B}(\mathbf{s}', \mathbf{a}'))$$

if the two Q's are noisy in *different* ways, there is no problem

Double Q-learning in practice

where to get two Q-functions?

just use the current and target networks!

standard Q-learning: $y = r + \gamma Q_{\phi'}(\mathbf{s}', \arg \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}', \mathbf{a}'))$

double Q-learning: $y = r + \gamma Q_{\phi'}(\mathbf{s}', \arg \max_{\mathbf{a}'} (\phi \phi', \mathbf{a}'))$

just use current network (not target network) to evaluate action still use target network to evaluate value!

Multi-step returns

these are the only values that matter if $Q_{\phi'}$ is bad! these values are important if $Q_{\phi'}$ is good

where does the signal come from?

Q-learning does this: max bias, min variance

remember this?
Actor-critic:
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \left(r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) + \gamma \hat{V}_{\phi}^{\pi}(\mathbf{s}_{i,t+1}) - \hat{V}_{\phi}^{\pi}(\mathbf{s}_{i,t}) \right)$$

+ lower variance (due to critic)
- not unbiased (if the critic is not perfect)
Policy gradient: $\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \left(\left(\sum_{t'=t}^{T} \gamma^{t'-t} r(\mathbf{s}_{i,t'}, \mathbf{a}_{i,t'}) \right) - b \right)$

+ no bias - higher variance (because single-sample estimate)

can we construct multi-step targets, like in actor-critic?

Q-learning target: $y_{j,t} = r_{j,t} + \gamma \max_{\mathbf{a}_{j,t+1}} Q_{\phi'}(\mathbf{s}_{j,t+1}, \mathbf{a}_{j,t+1})$

$$y_{j,t} = \sum_{t'=t}^{t+N-1} \gamma^{t-t'} r_{j,t'} + \gamma^N \max_{\mathbf{a}_{j,t+N}} Q_{\phi'}(\mathbf{s}_{j,t+N}, \mathbf{a}_{j,t+N})$$

N-step return estimator

Q-learning with N-step returns

$$y_{j,t} = \sum_{t'=t}^{t+N-1} \gamma^{t-t'} r_{j,t'} + \gamma^N \max_{\mathbf{a}_{j,t+N}} Q_{\phi'}(\mathbf{s}_{j,t+N}, \mathbf{a}_{j,t+N})$$

this is supposed to estimate $Q^{\pi}(\mathbf{s}_{j,t}, \mathbf{a}_{j,t})$ for π

$$\pi(\mathbf{a}_t | \mathbf{s}_t) = \begin{cases} 1 \text{ if } \mathbf{a}_t = \arg \max_{\mathbf{a}_t} Q_\phi(\mathbf{s}_t, \mathbf{a}_t) \\ 0 \text{ otherwise} \end{cases}$$

- + less biased target values when Q-values are inaccurate
- + typically faster learning, especially early on
- only actually correct when learning on-policy

we need transitions $\mathbf{s}_{j,t'}, \mathbf{a}_{j,t'}, \mathbf{s}_{j,t'+1}$ to come from π for t' - t < N - 1(not an issue when N = 1)

how to fix?

- ignore the problem
 - often works very well
 - cut the trace dynamically choose N to get only on-policy data

why?

- works well when data mostly on-policy, and action space is small
- importance sampling

For more details, see: "Safe and efficient off-policy reinforcement learning." Munos et al. '16

Q-learning with continuous actions

What's the problem with continuous actions?

$$\pi(\mathbf{a}_t|\mathbf{s}_t) = \begin{cases} 1 \text{ if } \mathbf{a}_t = \arg \max_{\mathbf{a}_t} Q_{\phi}(\mathbf{s}_t, \mathbf{a}_t) & \text{this max} \\ 0 \text{ otherwise} & \\ target \text{ value } y_j = r_j + \gamma \max_{\mathbf{a}'_j} Q_{\phi'}(\mathbf{s}'_j, \mathbf{a}'_j) & \text{this max} \\ particularly problematic (inner loop of training) & \\ particularly$$

How do we perform the max?

Option 1: optimization

- gradient based optimization (e.g., SGD) a bit slow in the inner loop
- action space typically low-dimensional what about stochastic optimization?

Q-learning with stochastic optimization

Simple solution:

 $\max_{\mathbf{a}} Q(\mathbf{s}, \mathbf{a}) \approx \max \left\{ Q(\mathbf{s}, \mathbf{a}_1), \dots, Q(\mathbf{s}, \mathbf{a}_N) \right\}$

 $(\mathbf{a}_1, \ldots, \mathbf{a}_N)$ sampled from some distribution (e.g., uniform)

but... do we care? How good does the target need to be anyway?

More accurate solution:

- cross-entropy method (CEM)
 - simple iterative stochastic optimization
- CMA-ES
 - substantially less simple iterative stochastic optimization

+ dead simple

- + efficiently parallelizable
- not very accurate

works OK, for up to about 40 dimensions

Easily maximizable Q-functions

Option 2: use function class that is easy to optimize

$$Q_{\phi}(\mathbf{s}, \mathbf{a}) = -\frac{1}{2} (\mathbf{a} - \mu_{\phi}(\mathbf{s}))^T P_{\phi}(\mathbf{s}) (\mathbf{a} - \mu_{\phi}(\mathbf{s})) + V_{\phi}(\mathbf{s})$$



NAF: Normalized Advantage Functions

$$\arg\max_{\mathbf{a}} Q_{\phi}(\mathbf{s}, \mathbf{a}) = \mu_{\phi}(\mathbf{s}) \qquad \max_{\mathbf{a}} Q_{\phi}(\mathbf{s}, \mathbf{a}) = V_{\phi}(\mathbf{s})$$

- + no change to algorithm
- + just as efficient as Q-learning
- loses representational power

Q-learning with continuous actions

Option 3: learn an approximate maximizer

DDPG (Lillicrap et al., ICLR 2016)

"deterministic" actor-critic (really approximate Q-learning)

 $\max_{\mathbf{a}} Q_{\phi}(\mathbf{s}, \mathbf{a}) = Q_{\phi}(\mathbf{s}, \arg \max_{\mathbf{a}} Q_{\phi}(\mathbf{s}, \mathbf{a}))$

idea: train another network $\mu_{\theta}(\mathbf{s})$ such that $\mu_{\theta}(\mathbf{s}) \approx \arg \max_{\mathbf{a}} Q_{\phi}(\mathbf{s}, \mathbf{a})$

how? just solve $\theta \leftarrow \arg \max_{\theta} Q_{\phi}(\mathbf{s}, \mu_{\theta}(\mathbf{s}))$ $\frac{dQ_{\phi}}{d\theta} = \frac{d\mathbf{a}}{d\theta} \frac{dQ_{\phi}}{d\mathbf{a}}$

new target $y_j = r_j + \gamma Q_{\phi'}(\mathbf{s}'_j, \mu_{\theta}(\mathbf{s}'_j)) \approx r_j + \gamma Q_{\phi'}(\mathbf{s}'_j, \arg \max_{\mathbf{a}'} Q_{\phi'}(\mathbf{s}'_j, \mathbf{a}'_j))$

Q-learning with continuous actions

Option 3: learn an approximate maximizer

DDPG:

1. take some action a_i and observe (s_i, a_i, s'_i, r_i), add it to β
2. sample mini-batch {s_j, a_j, s'_j, r_j} from β uniformly
3. compute y_j = r_j + γ max_{a'_j} Q_{φ'}(s'_j, μ_{θ'}(s'_j)) using target nets Q_{φ'} and μ_{θ'}
4. φ ← φ − α ∑_j dQ_φ/dφ (s_j, a_j)(Q_φ(s_j, a_j) − y_j)
5. θ ← θ + β ∑_j dμ/dθ (s_j) dQ_φ/da (s_j, a)
6. update φ' and θ' (e.g., Polyak averaging)

Simple practical tips for Q-learning

- Q-learning takes some care to stabilize
 - Test on easy, reliable tasks first, make sure your implementation is correct



Figure: From T. Schaul, J. Quan, I. Antonoglou, and D. Silver. "Prioritized experience replay". *arXiv preprint arXiv:1511.05952* (2015), Figure 7

- Large replay buffers help improve stability
 - Looks more like fitted Q-iteration
- It takes time, be patient might be no better than random for a while
- Start with high exploration (epsilon) and gradually reduce

Advanced tips for Q-learning

• Bellman error gradients can be big; clip gradients or user Huber loss

$$L(x) = \begin{cases} x^2/2 & \text{if } |x| \le \delta \\ \delta |x| - \delta^2/2 & \text{otherwise} \end{cases}$$



- Double Q-learning helps *a lot* in practice, simple and no downsides
- N-step returns also help a lot, but have some downsides
- Schedule exploration (high to low) and learning rates (high to low), Adam optimizer can help too
- Run multiple random seeds, it's very inconsistent between runs

Review

- Q-learning in practice
 - Replay buffers
 - Target networks
- Generalized fitted Q-iteration
- Double Q-learning
- Multi-step Q-learning
- Q-learning with continuous actions
 - Random sampling
 - Analytic optimization
 - Second "actor" network



Fitted Q-iteration in a latent space

- "Autonomous reinforcement learning from raw visual data," Lange & Riedmiller '12
- Q-learning on top of latent space learned with autoencoder
- Uses fitted Q-iteration
- Extra random trees for function approximation (but neural net for embedding)





IEEE-1394

Q-learning with convolutional networks

- "Human-level control through deep reinforcement learning," Mnih et al. '13
- Q-learning with convolutional networks
- Uses replay buffer and target network
- One-step backup
- One gradient step
- Can be improved a lot with double Q-learning (and other tricks)



Q-learning with continuous actions

- "Continuous control with deep reinforcement learning," Lillicrap et al. '15
- Continuous actions with maximizer network
- Uses replay buffer and target network (with Polyak averaging)
- One-step backup
- One gradient step per simulator step



Q-learning on a real robot

- "Robotic manipulation with deep reinforcement learning and ...," Gu*, Holly*, et al. '17
- Continuous actions with NAF (quadratic in actions)
- Uses replay buffer and target network
- One-step backup
- Four gradient steps per simulator step for efficiency
- Parallelized across multiple robots





Kalashnikov, Irpan, Pastor, Ibarz, Herzong, Jang, Quillen, Holly, Kalakrishnan, Vanhoucke, Levine. **QT-Opt: Scalable Deep Reinforcement Learning of Vision-Based Robotic Manipulation Skills**

minimize
$$\sum_{i} (Q(\mathbf{s}_i, \mathbf{a}_i) - [r(\mathbf{s}_i, \mathbf{a}_i) + \max_{\mathbf{a}'_i} Q(\mathbf{s}'_i, \mathbf{a}'_i)])^2$$

Q-learning suggested readings

- Classic papers
 - Watkins. (1989). Learning from delayed rewards: introduces Q-learning
 - Riedmiller. (2005). Neural fitted Q-iteration: batch-mode Q-learning with neural networks
- Deep reinforcement learning Q-learning papers
 - Lange, Riedmiller. (2010). Deep auto-encoder neural networks in reinforcement learning: early image-based Q-learning method using autoencoders to construct embeddings
 - Mnih et al. (2013). Human-level control through deep reinforcement learning: Qlearning with convolutional networks for playing Atari.
 - Van Hasselt, Guez, Silver. (2015). Deep reinforcement learning with double Q-learning: a very effective trick to improve performance of deep Q-learning.
 - Lillicrap et al. (2016). Continuous control with deep reinforcement learning: continuous Q-learning with actor network for approximate maximization.
 - Gu, Lillicrap, Stuskever, L. (2016). Continuous deep Q-learning with model-based acceleration: continuous Q-learning with action-quadratic value functions.
 - Wang, Schaul, Hessel, van Hasselt, Lanctot, de Freitas (2016). Dueling network architectures for deep reinforcement learning: separates value and advantage estimation in Q-function.